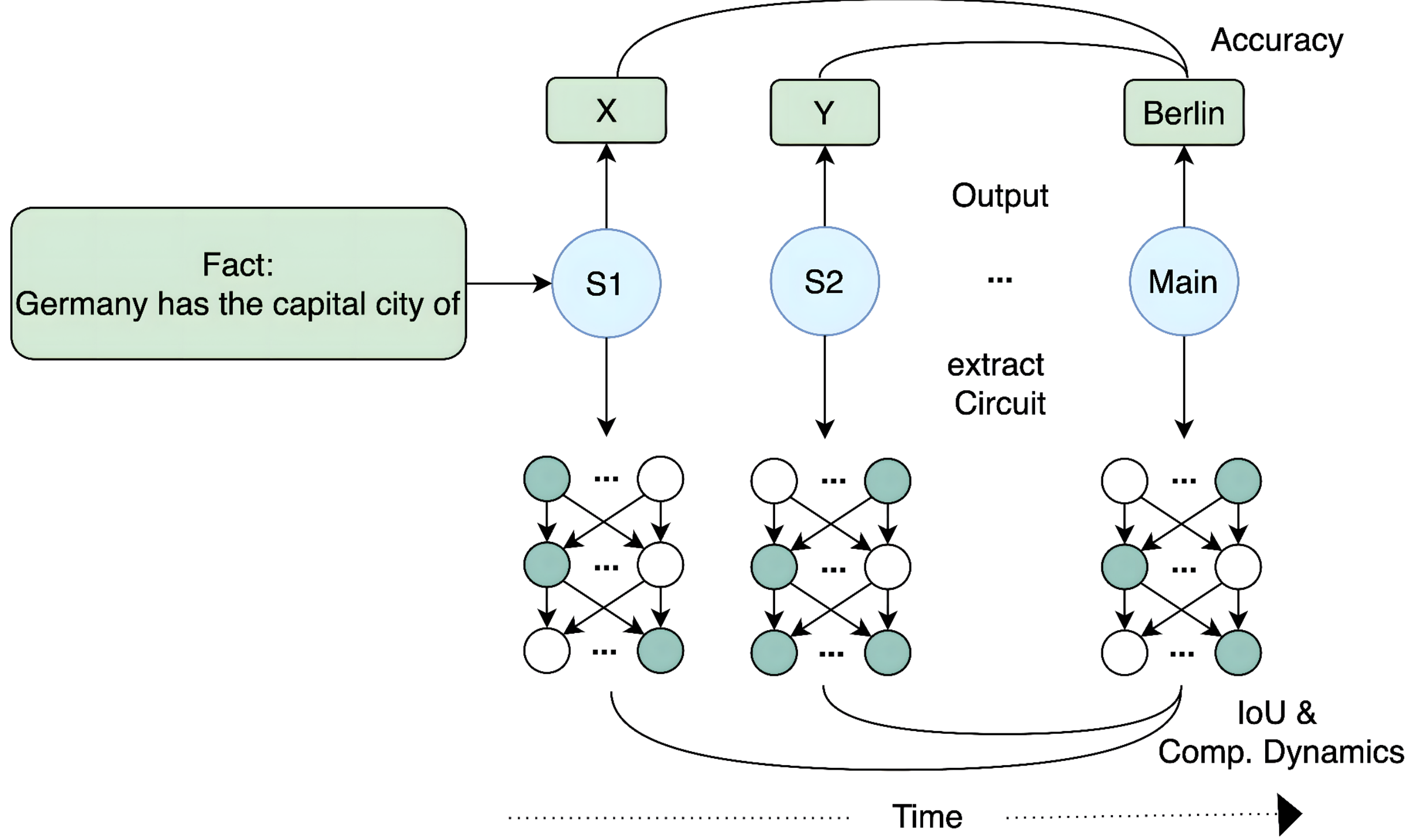


How does factual knowledge emerge during LLM pretraining?



- LLMs encode factual knowledge, yet the learning process remains opaque.
- Mechanistic interpretability methods let us identify the specific model components, namely attention heads and FFNs, that drive factual recall.
- This study traces the *evolution* of these components over 40 snapshots of OLMo-7B.

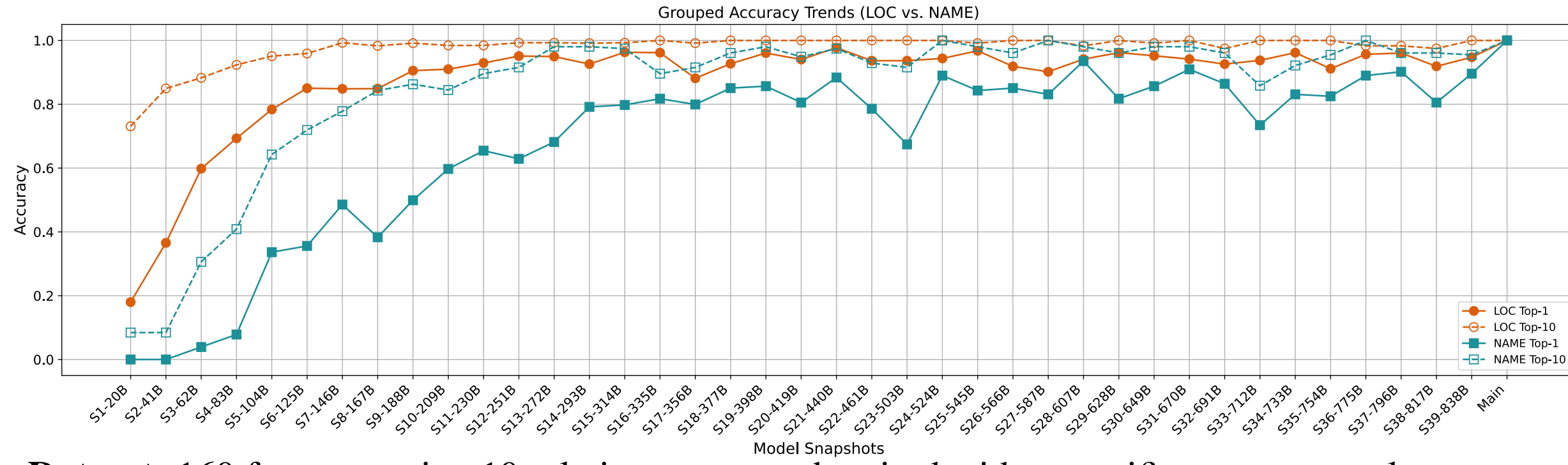
MAIN Findings:

- Task Complexity Influences Training Dynamics:** Simple facts (e.g. locations) converge early in pre-training, while more complex relationships (e.g., names) only emerge after sustained training.
- Hierarchical Learning Process:** The model initially leverages broad, general-purpose attention heads and FFNs before progressively spawning specialized submodules dedicated to narrower fact types.
- Adaptive vs. Stable Components:** A subset of attention heads dynamically repurposes throughout training to capture new information, whereas certain FFNs form a stable backbone that supports factual recall.
- Evolving Specialization:** Both attention heads and FFNs increasingly refine their roles, becoming more reliably tuned to specific categories of knowledge as training advances.

Dataset Construction

Germany has the capital city of Berlin

SUBJECT	RELATION	END	ANSWER
Location-based Relations (LOC)			
Relation	Prompt Template	# Facts	Example Subject
CITY_IN_COUNTRY	{ } is part of the country of	14	Rio de Janeiro, Buenos Aires
COMPANY_HQ	The headquarters of { } are in the city of	20	Zillow, Bayerischer Rundfunk
COUNTRY_CAPITAL_CITY	{ } has the capital city of	19	Canada, Nigeria
FOOD_FROM_COUNTRY	{ } is from the country of	17	Sushi, Ceviche
OFFICIAL_LANGUAGE	In { }, the official language is	14	France, Egypt
PLAYS_SPORT	{ } plays professionally in the sport of	12	Kobe Bryant, Roger Federer
SIGHTS_IN_CITY	{ } is a landmark in the city of	17	The Eiffel Tower, The Space Needle
Name-based Relations (NAME)			
Relation	Prompt Template	# Facts	Example Subject
BOOKS_WRITTEN	The Book { } was written by the author with the name of	13	The Hunger Games, Life of Pi
COMPANY_CEO	Who is the CEO of { }? Their name is	17	Ubisoft, Pinterest
MOVIE_DIRECTED	The Movie { } was directed by the director with the name of	17	The Godfather, Forrest Gump



- Dataset:** 160 facts spanning 10 relation types, each paired with a specific prompt template to guarantee correct, unambiguous completions by the model.
- Accuracy Trends:** Location-based facts reach near-perfect performance within the first few checkpoints, while name-based facts improve steadily across all 40 snapshots.

Model Component Roles

Role Score: $c_s^g = \frac{\sum_{r \in R} \sum_{f \in F} c_{srf}(T_g)}{\sum_{r \in R} \sum_{f \in F} 1}$

General: $\mathcal{H}_g = \mathcal{J}_g$

Entity: $c_s^e = \frac{\sum_{r \in R} \sum_{f \in F} c_{srf}(T_e)}{\sum_{r \in R} \sum_{f \in F} 1}$

Entity: $\mathcal{H}_e = \mathcal{J}_e - \mathcal{J}_g$

Relation-Answer: $c_s^r = \frac{\sum_{f \in F} c_{srf}(T_a)}{\sum_{f \in F} 1}$

Relation-Answer: $\mathcal{H}_r = \mathcal{J}_r - \mathcal{J}_e - \mathcal{J}_g$

Fact-Answer Specific: $c_s^f = c_{srf}^f(T_a)$

Fact-Answer Specific: $\mathcal{H}_f = \mathcal{J}_f - \mathcal{J}_r - \mathcal{J}_e - \mathcal{J}_g$

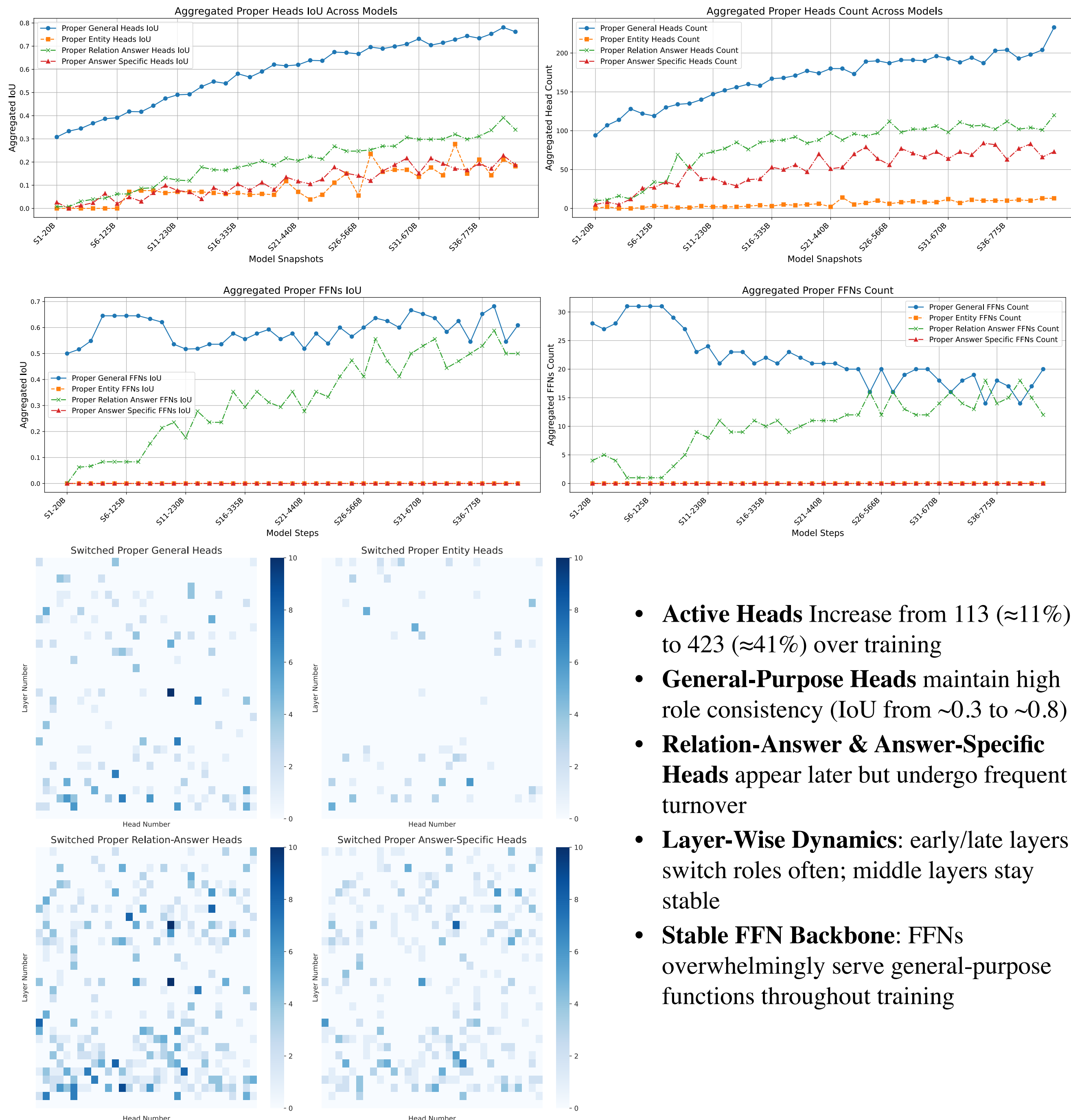
Deactivated Components: $\mathcal{H}_d = \mathcal{C}(\mathcal{H}_g \cup \mathcal{H}_e \cup \mathcal{H}_r \cup \mathcal{H}_f)$

- Extract per-subtoken circuits using Information Flow Routes (Ferrando & Voita, 2024)
- We compute activation scores $c_s^g, c_s^e, c_s^r, c_s^f$ for each component at each snapshot, using subtoken sets T_g, T_e, T_a , and a threshold $\theta = 0.1$.
- Then by successive differencing of cumulative importance sets $\mathcal{J}_g \rightarrow \mathcal{J}_e \rightarrow \mathcal{J}_r \rightarrow \mathcal{J}_f$, we obtain non-overlapping proper role sets $\mathcal{H}_g, \mathcal{H}_e, \mathcal{H}_r$ and \mathcal{H}_f , with \mathcal{H}_d capturing all remaining deactivated components.

How do Components Evolve?

Temporal Consistency and Role Dynamics of Components

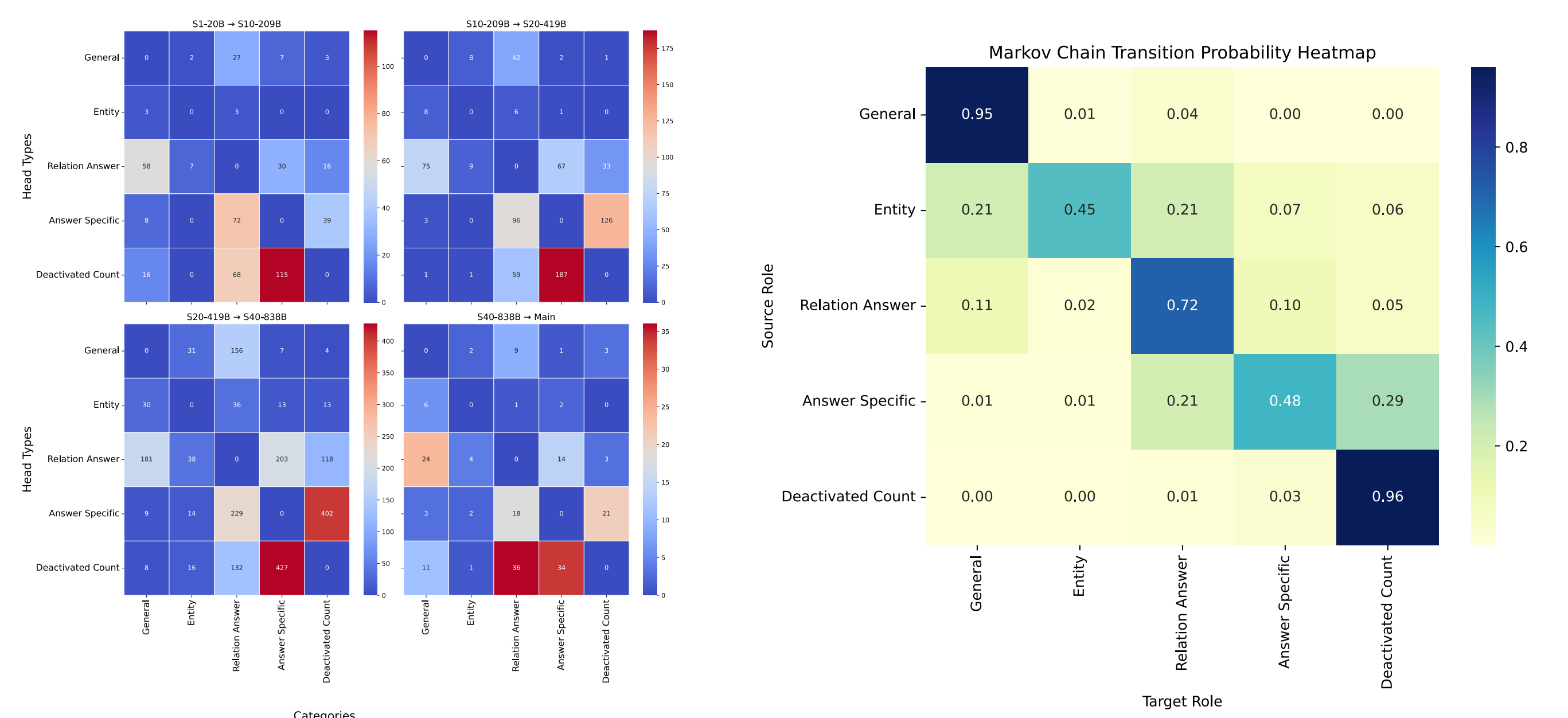
$$\text{IoU}(\mathcal{H}_g) = \frac{\mathcal{H}_{gs} \cap \mathcal{H}_{gmain}}{\mathcal{H}_{gs} \cup \mathcal{H}_{gmain}}$$



- Active Heads** Increase from 113 ($\approx 11\%$) to 423 ($\approx 41\%$) over training
- General-Purpose Heads** maintain high role consistency (IoU from ~ 0.3 to ~ 0.8)
- Relation-Answer & Answer-Specific Heads** appear later but undergo frequent turnover
- Layer-Wise Dynamics:** early/late layers switch roles often; middle layers stay stable
- Stable FFN Backbone:** FFNs overwhelmingly serve general-purpose functions throughout training

Dynamic Specialization and Generalization of Attention Heads

$$P(\mathcal{H}_\alpha \rightarrow \mathcal{H}_\beta) = \frac{N(\mathcal{H}_\alpha \rightarrow \mathcal{H}_\beta)}{\sum_{\gamma \in \{g, e, r, f, d\}} N(\mathcal{H}_\alpha \rightarrow \mathcal{H}_\gamma)}$$

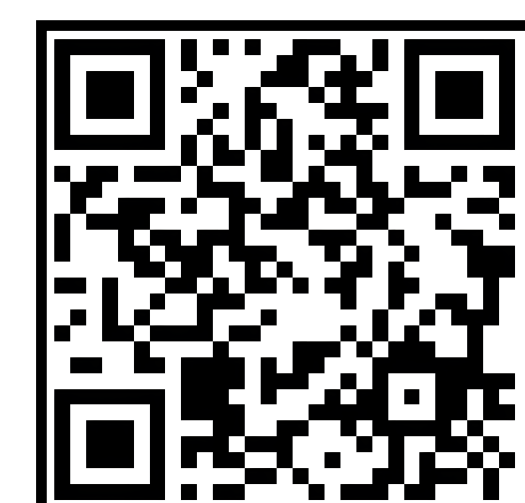


- Frequent Role Cycling:** Many heads repeatedly switch from inactive to specialized states (particularly answer-specific), then deactivate again, while general-purpose heads stay stable or migrate into relation-answer roles.
- Markov-Modeled Dynamics:** Specialized heads often revert to general roles, but new specializations emerge faster than they deactivate.
- Net Specialization Growth:** The total number of specialized heads increases steadily during training.

Code



Paper



Poster

